Dit tentamen is in elektronische vorm beschikbaar gemaakt door de $\mathcal{T}_{\mathcal{BC}}$ van A-Eskwadraat. A-Eskwadraat kan niet aansprakelijk worden gesteld voor de gevolgen van eventuele fouten in dit tentamen.

Department of Information and Computing Sciences Utrecht University

INFOB3TC- Exam 2

Sean Leather

Monday, 30 January 2012, 17:00 – 20:00

1 Preliminaries

- The exam consists of 8 pages (including this page). Please verify that you received all pages.
- Write your name and student number on all submitted work. Also include the total number of separate sheets of paper.
- The maximum score is stated at the top of each question. The total amount of points you can get is 195.
- Give simple and concise answers. Write readable text. Do not use pencils or pens with red ink.
- Write your text in English.
- When writing grammar and language constructs, you may use any set, sequence, or language operations covered during the course.
- When writing Haskell code, you may use functions from the *Prelude* and the following modules: *Data.Char*, *Data.List*, *Data.Maybe*, and *Control.Applicative*. If you are in doubt whether a certain function is allowed, please ask.
- Use your time efficiently. Look over all the questions, and answer the ones you know first.

IMPORTANT! Generally, you are allowed to take the resit exam if you have at least an average score of 4 on the exams. However, you can also take the resit if you do not submit this exam.

I will post the solutions tonight. If you look over the solutions and decide you want to "cancel" your submission, send an email to <code>leather@cs.uu.nl</code> by 14:00 tomorrow (Tuesday, 31 January 2012) indicating this.

Good luck!

2 Questions

2.1 Regular Languages

1 (5+5 points). Consider the following regular grammars for languages L_1 and L_2 :

$$L_1: S \to ab \mid cdS$$

$$L_2: S \to S A \mid \varepsilon$$

$$A \to abcd \mid dcba$$

- (a) Give a regular expression for each language.
- (b) Define a parser for each regular expression using the Haskell Regex combinator library described in Section 3.1. The parsers should produce an appropriate representation of the input.

 ${f 2}$ (15+15 points). For each language definition below, show whether or not the language is regular. If it is regular, give one of the following:

- (a) a regular grammar in an acceptable form,
- (b) a regular expression, or
- (c) a finite state automaton.

If the language is not regular, prove that using the pumping lemma for regular languages.

(a)
$$\{o^m p^n \mid n = m + 1\}$$

(b)
$$\{3^j7^k \mid j > 2, k < 5\}$$

2.2 Simple Stack Machine

3 (15 points). Translate this program into SSM instructions. See the SSM instruction set reference in Section 3.2.

```
void main() {
   int x = fib(4);
   fib(x);
}
int fib(int n) {
   if (n < 2)
     return 1;
   else
     return fib(n - 1) + fib(n - 2);
}</pre>
```

4 (10 points). Given the initial SSM register state below, show the final (relative) state after the above instructions have been executed (and just before the program finishes). You may assume that the code and stack memory do not share address space.

Register	Initial Value	Description of Initial Value
PC	i	First instruction address
SP	S	Current head of stack
MP	m	Unknown
RR	r	Unknown

3

2.3 LL Parsing

5 (30 points). Copy the table below and complete it by computing the values in the columns for the appropriate rows. Use *True* and *False* for property values and set notation for everything else.

NT	Production	empty	emptyRhs	first	firstRhs	follow	lookAhead
M							
	$M \rightarrow \langle E \rangle M$						
	$M o \varepsilon$						
Ε							
	$E \rightarrow Q$						
	$E \rightarrow Q; E$						
Q							
	$Q \rightarrow 0$						
	$Q \rightarrow 1$						
	$Q \rightarrow M$						

6 (15 points). Is the above grammar LL(1)? Explain how you arrived at your answer. If the grammar is not LL(1), transform the grammar such that is LL(1) and complete a new table with only the rows that differ from the old table.

7 (15 points). Show the steps that a parser for the above LL(1) grammar (after transformation if necessary) goes through to recognize the following input sequence:

For each step (one per line), show the stack, the remaining input, and the action (followed by the relevant symbol or production) performed. If you reach a step in which you cannot proceed, note the action as "error."

2.4 LR Parsing

8 (25 points). Copy the table below and complete it by computing the values in the columns for the appropriate rows. Where the label "(set)" is given, use set notation. Where "(RE)" is given, use regular expression notation. A set may reference other sets – using [X] as the notation for the left context set of X – but a regular expression must not reference other regular expressions.

NT	Production	Left Context (set)	Left Context (RE)	LR(0) Context (RE)
S				
	$S \to As$			
\boldsymbol{A}				
	$A \rightarrow A\%B$			
	$A \rightarrow B$			
В				
	$B \to b$ $B \to aA$			
	$B \to aA$			

9 (15 points). Is the above grammar LR(0)? Explain how you arrived at your answer. If the grammar is not LR(0), transform the grammar such that is LR(0) and complete a new table with only the rows that differ from the old table.

10 (15 points). Construct the deterministic LR(0) automaton (characteristic machine) for the above LR(0) grammar (after transformation if necessary). Clearly label the start state, transitions, and accepting states.

11 (15 points). Show the steps that a parser for the above LR(0) grammar (after transformation if necessary) goes through to recognize the following input sequence:

ab%abas

For each step (one per line), show the stack, the remaining input, and the action (followed by the relevant symbol or production) performed. If you reach a step in which you cannot proceed, note the action as "error."

Note: You may use either symbols alone or symbols along with states from your DFA above, as you like.

3 Appendix

3.1 Regular Expression Combinators

The following is the interface to a small regular expression parser combinator library. It centers around the abstract *Regex* datatype. The combinators are built from standard Haskell library type classes: *Functor*, *Applicative*, and *Alternative*. The semantics of each function should be clear from its name, type, and your experience with similar parser combinator libraries.

```
data Regex s a = ...
instance Functor (Regex s) where...
instance Applicative (Regex s) where ...
instance Alternative (Regex s) where ...
class (Functor f) \Rightarrow Applicative f where
   pure :: a \rightarrow f a
   (<*>) :: f(a \rightarrow b) \rightarrow fa \rightarrow fb
   (*>) :: fa \rightarrow fb \rightarrow fb

(<*) :: fa \rightarrow fb \rightarrow fa
class (Applicative f) \Rightarrow Alternative f where
   empty :: f a
   (\langle | \rangle) :: f a \rightarrow f a \rightarrow f a
   some :: f a \rightarrow f [a]
   many :: f a \rightarrow f [a]
satisfy :: (s \rightarrow Bool) \rightarrow Regex s s
symbol :: (Eq s) \Rightarrow s \rightarrow Regex s s
run :: Regex s a \rightarrow [s] \rightarrow Maybe a
```

3.2 SSM Reference

SSM instructions are given in textual form, called assembler notation. For this exam, a program is a sequence of instructions with each instruction on a separate line, optionally proceed by a label and a colon (e.g. main:). A label (e.g. main) may be used as an argument to an instruction.

Copying Instructions

Instructions	Description
ldc	Load a constant
lds	Load a value relative to the SP
ldh	Load a value relative to the HP
ldl	Load a value relative to the MP
lda	Load a value pointed to by the value on top of the stack
ldr	Load a register value
ldrr	Load a register with a value from another register
ldsa	Load address of value relative to the SP
ldla	Load address of value relative to the MP
ldaa	Load address of value relative to the address on top of the stack
sts	Store a value relative to the SP
sth	Store a value relative to the HP
stl	Store a value relative to the MP
sta	Store a value pointed to by a value on the stack
str	Store a value in a register

Convenience Instructions For the Stack

Instructions	Description
ajs	Adjust the SP
link	Save the MP, adjust the MP and SP suitable for programming language function entry
unlink	Reverse of link

Arithmetic Instructions

Instructions	Description	
add, sub, mul, div, mod, neg, and, or, xor	Binary operations	
not	Unary operation Put an int value on the stack which is interpreted as a status register value containing condition code to be used by a branch instruction	
eq, ne, lt, gt, le, ge	Put true value on the stack if comparison is true	

Control Instructions

Instructions	Description		
beq, bne, blt, bgt, ble, bge	Branch on equality, unequality, less than, greater than, less or equal, greater or equal. These instructions pop the stack, interpret it as a condition code and jump accordingly		
bra	Branch always, no popping of the stack		
brf (brt)	Branch if top of stack is false (true)		
bsr	Branch to subroutine. Like bra, but pushes the previous PC be-		
	fore jumping		
jsr	Jump to subroutine. Like bsr, but pops its destination from the		
5	stack		